Homogeneity or implicature An experimental study of free choice

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Implicatures and their boundaries

• What should we treat as implicatures?

Implicatures and their boundaries

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- Plural definites
- Bare plurals
- Neg-raising
- Temporal inferences
- Free choice
- . . .

The focus

- Plural definites
- Bare plurals
- Neg-raising
- Temporal inferences
- Free choice
- . . .

Today

The question: Is Free choice an implicature?



Experimental project directly addressing this question

Outline

1 Overview

2 Background

Free choice and Dual prohibition The implicature approach The homogeneity approach

- **3** Predictions
- 4 The experiment

Results

5 Discussion

The main result Wide scope disjunction Further directions

6 Conclusion

Addressing the challenge

What is free choice?¹

(1) Angie is allowed to buy the car or the boat.

¹von Wright 1968, Kamp 1974

What is free choice?¹

Angie is allowed to buy the car or the boat. → Angie can choose between the two

¹von Wright 1968, Kamp 1974

Disappearing under negation

(2) Angie is not allowed to buy the car or the boat.

Disappearing under negation

(2) Angie is not allowed to buy the car or the boat.

 → It's not true that Angie can choose between the two

Disappearing under negation

Two main approaches

Implicature based
 Non-implicature based

The goal

Testing a clear divergent prediction of the two approaches

The main result

A challenge for the implicature approach

Why does it matter?

• Tells us something about theories of free choice

Why does it matter?

- Tells us something about theories of free choice
- Potentially about implicatures as well

Why does it matter?

- Tells us something about theories of free choice
- Potentially about implicatures as well
- Experimentally distinguishes between theories

1 Background

1 Background

2 The two approaches

- 1 Background
- 2 The two approaches
- **3** The divergent prediction

- Background
- 2 The two approaches
- **3** The divergent prediction
- 4 The experiment

- Background
- **2** The two approaches
- **3** The divergent prediction
- 4 The experiment
- **5** Discussion and conclusion

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Free choice

(3) Angie is allowed to buy the car or the boat. → Angie can choose between the two

Under negation

(5) $\Diamond (A \lor B)$

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$(5) \qquad \Diamond (\mathsf{A} \lor \mathsf{B}) \leadsto \Diamond \mathsf{A} \land \Diamond \mathsf{B}$

FREE CHOICE

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$$(5) \qquad \Diamond (\mathsf{A} \lor \mathsf{B}) \rightsquigarrow \Diamond \mathsf{A} \land \Diamond \mathsf{B}$$

FREE CHOICE

$$(6) \qquad \neg \Diamond (\mathsf{A} \lor \mathsf{B}) \rightsquigarrow \neg \Diamond \mathsf{A} \land \neg \Diamond \mathsf{B}$$

$$(5) \qquad \Diamond (\mathsf{A} \lor \mathsf{B}) \rightsquigarrow \Diamond \mathsf{A} \land \Diamond \mathsf{B}$$

$$(6) \qquad \neg \Diamond (\mathsf{A} \lor \mathsf{B}) \rightsquigarrow \neg \Diamond \mathsf{A} \land \neg \Diamond \mathsf{B}$$

FREE CHOICE DUAL PROHIBITION

The empirical puzzle

• How free choice arises in positive contexts

The empirical puzzle

- How free choice arises in positive contexts
- How dual prohibition arises in negative contexts

Two main approaches

- 1 Implicature based
- 2 Non-implicature based

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The implicature approach²

• Free choice is an implicature

²Fox 2007, Klinedinst 2006, Chierchia 2013, Chemla 2010, Franke 2013, Santorio & Romoli 2018, Bar-Lev & Fox 2017 a.o
The implicature approach $^{2} \$

- Free choice is an implicature
- Dual prohibition is just part of the literal meaning

²Fox 2007, Klinedinst 2006, Chierchia 2013, Chemla 2010, Franke 2013, Santorio & Romoli 2018, Bar-Lev & Fox 2017 a.o

(7)
$$\Diamond (\mathsf{A} \lor \mathsf{B}) = \Diamond \mathsf{A} \lor \Diamond \mathsf{B}$$

LITERAL MEANING

(7)
$$\Diamond (A \lor B) = \Diamond A \lor \Diamond B$$

(8) $\neg \Diamond (A \lor B) = \neg \Diamond A \land \neg \Diamond B$

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(7)
$$\Diamond (\mathsf{A} \lor \mathsf{B}) = \Diamond \mathsf{A} \lor \Diamond \mathsf{B}$$

$$(8) \qquad \neg \Diamond (\mathsf{A} \lor \mathsf{B}) = \neg \Diamond \mathsf{A} \land \neg \Diamond \mathsf{B}$$

$$(9) \qquad \operatorname{IMP}[\Diamond(\mathsf{A} \lor \mathsf{B})] = \Diamond \mathsf{A} \land \Diamond \mathsf{B}$$

LITERAL MEANING DUAL PROHIB FREE CHOICE

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(7)
$$\Diamond(A \lor B) = \Diamond A \lor \Diamond B$$
LITERAL MEANING(8) $\neg \Diamond(A \lor B) = \neg \Diamond A \land \neg \Diamond B$ DUAL PROHIB(9)IMP[$\Diamond(A \lor B)$] = $\Diamond A \land \Diamond B$ FREE CHOICE(10) $* \neg IMP \Diamond(A \lor B)$) = $\neg \Diamond A \lor \neg \Diamond B$ NEGATED FREE CHOICE

- Free choice arises as an implicature
- Dual prohibition is just part of the literal meaning

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Addressing the challenge

Non-implicature accounts³

• The implicature approach is not the only option

³Aloni 2018, Starr 2016, Willer 2018, Goldstein 2018, Rothschild and Yablo 2018; see also Chemla 2010

Non-implicature accounts³

- The implicature approach is not the only option
- Non-implicature accounts of free choice

³Aloni 2018, Starr 2016, Willer 2018, Goldstein 2018, Rothschild and Yablo 2018; see also Chemla 2010

Non-implicature accounts³

- The implicature approach is not the only option
- Non-implicature accounts of free choice
- A recent account based on homogeneity for concreteness

³Aloni 2018, Starr 2016, Willer 2018, Goldstein 2018, Rothschild and Yablo 2018; see also Chemla 2010

The homogeneity approach: the gist⁴

• Free choice is just part of the literal meaning

⁴Goldstein 2018, Rothschild and Yablo 2018

The homogeneity approach: the gist⁴

- Free choice is just part of the literal meaning
- Dual prohibition arises via homogeneity

The homogeneity approach: the gist⁵

- Free choice is just part of the literal meaning
- Dual prohibition arises via a homogeneity presupposition

⁵Goldstein 2018, Rothschild and Yablo 2018

$$(11) \qquad \Diamond (\mathsf{A} \lor \mathsf{B}) = \Diamond \mathsf{A} \land \Diamond \mathsf{B}$$

FREE CHOICE

(11)
$$\Diamond (A \lor B) = \Diamond A \land \Diamond B$$

(12) $\Diamond A \leftrightarrow \Diamond B$

$$(11) \qquad \Diamond (\mathsf{A} \lor \mathsf{B}) = \Diamond \mathsf{A} \land \Diamond \mathsf{B}$$

$$(12) \qquad \Diamond \mathsf{A} \leftrightarrow \Diamond \mathsf{B}$$

(13)
$$\neg \Diamond (\mathsf{A} \lor \mathsf{B}) = \neg (\Diamond \mathsf{A} \land \Diamond \mathsf{B})$$

FREE CHOICE HOMOGENEITY NEGATED FREE CHOICE

(14)
$$\Diamond(A \lor B) = \Diamond A \land \Diamond B$$
FREE CHOICE(15) $\Diamond A \leftrightarrow \Diamond B$ HOMOGENEITY(16) $\neg \Diamond(A \lor B) = \neg(\Diamond A \land \Diamond B)$ NEGATED FREE CHOICE

(14)
$$\Diamond(A \lor B) = \Diamond A \land \Diamond B$$
FREE CHOICE(15) $\Diamond A \leftrightarrow \Diamond B$ HOMOGENEITY(16) $\neg \Diamond (A \lor B) = \neg(\Diamond A \land \Diamond B)$ NEGATED FREE CHOICE(17) $\neg \Diamond A \land \neg \Diamond B$ DUAL PROHIB

- Free choice is just part of the literal meaning
- Dual prohibition arises via the homogeneity presupposition

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Addressing the challenge

The two approaches

• Successfully capture basic pattern and more complex data

The two approaches

- Successfully capture basic pattern and more complex data
- Roughly with similar empirical coverage

A simple divergent prediction⁶

Distinguish between the two given a simple divergent prediction

⁶Kriz 2015, 2017, Tieu et al 2018

Free choice vs dual prohibition

- (18) Angie is allowed to buy the car or the boat
 → Angie can choose between the two FREE CHOICE
 (10) Angie is and allowed to be allowed to be added to be allowed to be added to be ad
- (19) Angie is not allowed to buy the car or the boat → Angie cannot buy either one DUAL PROHIB

The implicature approach

The implicature approach

- (20) Angie is allowed to buy the car or the boat → Angie can choose between the two IMPLICATURE
- (21) Angie is not allowed to buy the car or the boat → Angie cannot buy either one LITERAL MEANING

The homogeneity approach

(22) Angie is allowed to buy the car or the boat → Angie can choose between the two LITERAL MEANING

The homogeneity approach

- (23) Angie is not allowed to buy the car or the boat → Angie cannot buy either one (VIA) PRESUPPOSITION

The homogeneity approach

- (24) Angie is allowed to buy the car or the boat → Angie can choose one iff she can choose the other PRES
- (25) Angie is not allowed to buy the car or the boat → Angie can choose one iff she can choose the other PRES

Difference in status

Context: Angie is only allowed to buy the boat

(26) Angie is allowed to buy the car or the boat → Angie can choose between the two FALSE IMP

Difference in status

Context: Angie is only allowed to buy the boat

(27) Angie is not allowed to buy the car or the boat \rightsquigarrow Angie cannot buy either one FALSE

No difference in status

Context: Angie is only allowed to buy the boat

(28) Angie is allowed to buy the car or the boat → Angie can choose one iff she can choose the other PS FAIL

No difference in status

Context: Angie is only allowed to buy the boat

(29) Angie is not allowed to buy the car or the boat → Angie can choose one iff she can choose the other PS FAIL

	IMPLICATURE	HOMOGENEITY
POS	IMPLICATURE VIOLATION	PRESUPPOSITION FAILURE
NEG	FALSITY	PRESUPPOSITION FAILURE

	IMPLICATURE	HOMOGENEITY
POS	IMPLICATURE VIOLATION	PRESUPPOSITION FAILURE
NEG	FALSITY	PRESUPPOSITION FAILURE

• Testing these predictions
In sum

- Testing these predictions
- A simple way to distinguish between the two approaches

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The goal

• Testing the divergent predictions above

The goal

A ternary task building on previous work on implicatures, presuppositions, and homogeneity $^{7} \ \ \,$

⁷Kriz & Chemla 2016, Katsos and Bishop 2011, Abrusan and Szendroi 2013

Free choice - FC

(30) Angie is allowed to buy the car or the boat(31) Angie is not allowed to buy the car or the boat

Simple disjunction - OR

- (32) Angie bought the car or the boat
- (33) Angie didn't buy the car or the boat

Simple disjunction - OR

(34) Angie bought the car or the boat
 → Angie didn't buy both the car and the boat
 IMP

Simple disjunction - OR

(34) Angie bought the car or the boat

 → Angie didn't buy both the car and the boat
 IMP

 (35) Angie didn't buy the car or the boat

 → Angie didn't buy either
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The design

2x2 design with $\rm INFERENCE$ TYPE (FC vs OR; between) and $\rm POLARITY$ (within) as factors

Material: FC targets

Context: Angie is only allowed to buy the car

Material: FC targets

Context: Angie is only allowed to buy the car

- (36) Angie is allowed to buy the car or the boat
- (37) Angie is not allowed to buy the car or the boat

Material: OR targets

Context: Angie bought both the car and the boat

Material: OR targets

Context: Angie bought both the car and the boat

- (38) Angie bought the car or the boat
- (39) Angie didn't buy the car or the boat

Controls

- FC and OR
- Positive and negative
- True and false

Materials

• Each participant saw 8 targets and 8 controls in total

• Ternary judgment task with participants evaluating sentences attributed to a puppet against a scenario

- Ternary judgment task with participants evaluating sentences attributed to a puppet against a scenario
- The task is to choose a reward among three possible ones

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- The task is to choose a reward among three possible ones



Prediction mode: the sentences are puppet's guesses about

Prediction mode: the sentences are puppet's guesses about

what a character is allowed/not allowed to buy

FC

Prediction mode: the sentences are puppet's guesses about

- what a character is allowed/not allowed to buy FC
- what a character bought/didn't buy

OR

Example FC negative



Angie is not allowed to buy the car or the boat

Example FC negative



Example FC negative



Participants

- 114 participants recruited through AMT, randomly assigned to the two conditions
- 3 excluded for not reporting English as their native language, leaving 111 participants (56 in FC condition, 55 in disjunction condition)

Predictions - OR - both approaches



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Predictions - OR - both approaches



(40) Angie bought the car or the boat IMP FALSE(41) Angie didn't buy the car or the boat FALSE

Predictions - OR



- (42) Angie bought the car or the boat
- (43) Angie didn't buy the car or the boat



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Predictions - FC - implicature approach



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Predictions - FC - implicature approach



(44) Angie is allowed to buy the car or the boat IMP FALSE(45) Angie is not allowed to buy the car or the boat FALSE

Predictions - FC - implicature approach



- (46) Angie is allowed to buy the car or the boat
- (47) Angie isn't allowed to buy the car or the boat \P



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Predictions - FC - homogeneity approach



(48) Angie is allowed to buy the car or the boat PS FAIL(49) Angie is not allowed to buy the car or the boat PS FAIL

Predictions - FC - homogeneity approach



- (50) Angie is allowed to buy the car or the boat
- (51) Angie isn't allowed to buy the car or the boat



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Predictions - FC - homogeneity approach



(52) Angie is allowed to buy the car or the boat
(53) Angie isn't allowed to buy the car or the boat

In sum - Predictions

	OR	FC IMP	FC ном
POS	IMP VIOLATION	IMP VIOLATION	PS FAIL
NEG	FALSITY	FALSITY	PS FAIL

In sum - Predictions

	OR	FC IMP	FC ном
POS	IMP VIOLATION	IMP VIOLATION	PS FAIL
NEG	FALSITY	FALSITY	PS FAIL
In sum - Predictions

	OR	FC IMP	FC ном
POS	IMP VIOLATION	IMP VIOLATION	PS FAIL
NEG	FALSITY	FALSITY	PS FAIL

In sum - Predictions

	OR	FC IMP	FC ном
POS	IMP VIOLATION	IMP VIOLATION	PS FAIL
NEG	FALSITY	FALSITY	PS FAIL

Predictions - in sum

• An interaction between TYPE OF INFERENCE and POLARITY

Predictions - in sum

- An interaction between TYPE OF INFERENCE and POLARITY
- Challenging for the implicature approach

Predictions - in sum

- An interaction between TYPE OF INFERENCE and POLARITY
- Challenging for the implicature approach
- Entirely in line with the homogeneity approach

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Angie didn't buy the car or the boat

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Angie bought the car or the boat

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Angie is not allowed to buy the car or the boat



Results⁸



Effect of POLARITY ($\chi^2(1) = 102, p < .001$) Marginal effect of INFERENCE TYPE ($\chi^2(1) = 3.2, p = .07$)

⁸Mixed effects cumulative link model

Results⁹



Interaction between INFERENCE TYPE and POLARITY $(\chi^2(1) = 88, p < .001)$

⁹Mixed effects cumulative link model

In sum

• Interaction between type of inference and polarity

In sum

- Interaction between type of inference and polarity
- Difference between positive and negative with OR

In sum

- Interaction between type of inference and polarity
- Difference between positive and negative with OR
- Symmetric responses for positive and negative with FC

Controls



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• Participants' behavior on disjunction in line with previous studies

- · Participants' behavior on disjunction in line with previous studies
- Distinguished between falsity and implicature violation

- · Participants' behavior on disjunction in line with previous studies
- Distinguished between falsity and implicature violation
- Assigned intermediate status to both positive and negative for FC

• Challenging for the implicature approach

- Challenging for the implicature approach
- Entirely in line with the homogeneity approach

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• OR and FC are analogous in both positive and negative

- OR and FC are analogous in both positive and negative
- The FC negative condition has a true reading with wide scope disjunction





(54) Angie is not allowed to buy the car or the boat FALSE



- (54) Angie is not allowed to buy the car or the boat FALSE
- (55) Either Angie is not allowed to buy the car or she is not allowed to buy the boat TRUE



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(56) Angie didn't buy the car or the boat FALSE



- (56) Angie didn't buy the car or the boat FALSE
- (57) Either Angie did not buy the car or she did not buy the boat FALSE

Back to the results



Possible interpretation



When there is ambiguity and the truth-value of the readings are different, the intermediate value is $chosen^{10}$

¹⁰Bill et al 2018

Possible interpretation



The negative FC would be accounted for given this hypothesis
To test this hypothesis we need a baseline with OR and negation

- To test this hypothesis we need a baseline with OR and negation
- Where wide scope disjunction leads to a true reading





(58) Angie didn't buy the boat or the car FALSE

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- (58) Angie didn't buy the boat or the car FALSE
- (59) Either Angie did not buy the boat or she did not buy the car TRUE



FALSE TRUE

We have it already



Comparing it to the FC negative target



The comparison



The comparison



Marginally significant effect of inference type (z = 1.7, p = .08)

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The comparison



(62) Angie is not allowed to buy the car or the boat(63) Angie didn't buy the car or the boat

In sum

• Wide scope as an explanation of the difference between OR and FC negative?

In sum

- Wide scope as an explanation of the difference between OR and FC negative?
- The comparison with the OR control also reveals a difference

In sum

- Wide scope as an explanation of the difference between OR and FC negative?
- The comparison with the OR control also reveals a difference
- Scope might be playing a role but it can't be the whole story

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(64) Angie is allowed to buy the car or the boat

(64) Angie is allowed to buy the car or the boat → Angie is allowed to buy one iff she is allowed to buy the other

¹¹Kriz and Chemla 2015, Rothschild and Yablo 2018, Romoli and Santorio 2018

- (64) Angie is allowed to buy the car or the boat → Angie is allowed to buy one iff she is allowed to buy the other
- (65) If Angie is allowed to buy the car or the boat, she will choose the car.

¹¹Kriz and Chemla 2015, Rothschild and Yablo 2018, Romoli and Santorio 2018

- (64) Angie is allowed to buy the car or the boat → Angie is allowed to buy one iff she is allowed to buy the other
- (65) If Angie is allowed to buy the car or the boat, she will choose the car.
 ? → Angie is allowed to buy one iff she is allowed to buy the other

¹¹Kriz and Chemla 2015, Rothschild and Yablo 2018, Romoli and Santorio 2018

(66) Angie met the students

 12 Kriz and Chemla 2015, Rothschild and Yablo 2018, Romoli and Santorio 2018 <

(66) Angie met the students → Angie either met all or none of the students

¹²Kriz and Chemla 2015, Rothschild and Yablo 2018, Romoli and Santorio 2018

(66) Angie met the students → Angie either met all or none of the students

(67) If Angie met the students, she knows the situation.

¹²Kriz and Chemla 2015, Rothschild and Yablo 2018, Romoli and Santorio 2018

(66) Angie met the students → Angie either met all or none of the students

(67) If Angie met the students, she knows the situation.
 ? → Angie either met all or none of the students

¹²Kriz and Chemla 2015, Rothschild and Yablo 2018, Romoli and Santorio 2018

Adding a direct comparison with presuppositions¹³

- Adding a direct comparison with presuppositions¹³
- Context: The Pope isn't married

- Adding a direct comparison with presuppositions¹³
- Context: The Pope isn't married

(68) Angie is travelling with the Pope's wife

- Adding a direct comparison with presuppositions¹³
- Context: The Pope isn't married
 - (68) Angie is travelling with the Pope's wife
 - (69) Angie is not travelling with the Pope's wife

• Adding a direct comparison with plural definites¹⁴

- Adding a direct comparison with plural definites¹⁴
- Context: Angie met only half of the students

- Adding a direct comparison with plural definites¹⁴
- Context: Angie met only half of the students
 - (70) Angie met the students

- Adding a direct comparison with plural definites¹⁴
- Context: Angie met only half of the students
 - (70) Angie met the students
 - (71) Angie didn't meet the students

Extension to other populations

• 4-6-year-old children

Extension to other populations

- 4–6-year-old children
- Patients with psychosis¹⁵

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Conclusion

• Experimental work addressing the debate between implicature and non-implicature approaches to free choice

Conclusion

- Experimental work addressing the debate between implicature and non-implicature approaches to free choice
- Results are challenging for the implicature approach
Conclusion

• Either as supporting a non-implicature approach or as a push to refine the implicature one

Conclusion

- Either as supporting a non-implicature approach or as a push to refine the implicature one
- Powerful and simple perspective to address this debate

Conclusion

- Plural definites
- Bare plurals
- Neg-raising
- Temporal inferences
- . . .

Thanks!



Moysh Bar-Lev, Milica Denic, Simon Goldstein, Mora Maldonado, Paul Marty, Agata Renans, and Paolo Santorio

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Addressing the challenge

Addressing the challenge

• Appealing to differences among scalar items is not enough¹⁶

Addressing the challenge

Unclear that a difference between alternatives would help¹⁷

¹⁷Chemla and Bott 2013, Tieu et al 2016

Addressing the challenge

• Re-thinking the distribution of implicatures might help¹⁸

(72) Angie is not allowed to buy the car or the boat

(72) Angie is not allowed to buy the car or the boat(73) not[Angie is allowed to buy the car or the boat]

(72) Angie is not allowed to buy the car or the boat
 (73) not[Angie is allowed to buy the car or the boat]
 → Angie cannot buy either one

FALSE

(74) Angie is not allowed to buy the car or the boat
(75) not[IMP[Angie is allowed to buy the car or the boat]

(74) Angie is not allowed to buy the car or the boat
(75) not[IMP[Angie is allowed to buy the car or the boat]
→ it's not true that Angie can choose between the two

(74) Angie is not allowed to buy the car or the boat
 (75) not[IMP[Angie is allowed to buy the car or the boat]
 → it's not true that Angie can choose between the two TRUE

Context:
$$\Diamond A \land \neg \Diamond B$$
False(76) $\neg \Diamond (A \lor B) = \neg \Diamond A \land \neg \Diamond B$ False

Context:
$$\Diamond A \land \neg \Diamond B$$
FALSE(76) $\neg \Diamond (A \lor B) = \neg \Diamond A \land \neg \Diamond B$ FALSE(77) $\neg (IMP \Diamond (A \lor B)) = \neg (\Diamond A \land \Diamond B)$ TRUE

The interpretation as before

If one reading is true and one is false go for the intermediate value

Back to the results



The standard constraint

Do not weaken!: do not compute an implicature if it weakens the overall meaning of the sentence

(78)
$$\neg \Diamond (A \lor B) = \neg \Diamond A \land \neg \Diamond B$$
 False

(78)
$$\neg \Diamond (A \lor B) = \neg \Diamond A \land \neg \Diamond B$$
 FALSE
(79) $^*\neg (IMP \Diamond (A \lor B)) = \neg (\Diamond A \land \Diamond B)$ TRUE

Same for OR

$$(80) \qquad \neg (A \lor B) = \neg A \land \neg B$$

FALSE

Same for OR

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(80)
$$\neg (A \lor B) = \neg A \land \neg B$$
 FALSE
(81) $\neg (IMP(A \lor B)) = \neg [(A \lor B) \land \neg (A \land B)]$ TRUE

(81)
$$\neg(\operatorname{IMP}(A \lor B)) = \neg[(A \lor B) \land \neg(A \land B)]$$
 True

Same for OR

(82)
$$\neg(A \lor B) = \neg A \land \neg B$$
 FALSE
(83) $*\neg(IMP(A \lor B)) = \neg[(A \lor B) \land \neg(A \land B)]$ TRUE

A different principle¹⁹

Do not compute an implicature if it leads to a non-connected meaning

A different principle²⁰

• This principle can distinguish between FC and OR

A different principle²⁰

- This principle can distinguish between FC and OR
- The inference of disjunction under negation leads to a non-connected meaning

A different principle²⁰

- This principle can distinguish between FC and OR
- The inference of disjunction under negation leads to a non-connected meaning
- Free choice under negation leads to a connected meaning

A different principle

Context:
$$\Diamond A \land \neg \Diamond B$$

(84) $\neg \Diamond (A \lor B) = \neg \Diamond A \land \neg \Diamond B$ FALSE
(85) $\neg (IMP \Diamond (A \lor B)) = \neg (\Diamond A \land \Diamond B)$ TRUE

Different for OR

(86)
$$\neg (A \lor B) = \neg A \land \neg B$$
 FALSE
(87) $*\neg (IMP(A \lor B)) = \neg [(A \lor B) \land \neg (A \land B)]$ TRUE

Back to the results



(88) Angie didn't buy the car or the boat

(88) Angie didn't buy the car or the boat ... she didn't want either one

(88) Angie didn't buy the car or the boat . . . she didn't want either one EASY

- (88) Angie didn't buy the car or the boat ... she didn't want either one EASY
- (89) Angie didn't buy the car or the boat ...

- (88) Angie didn't buy the car or the boat ... she didn't want either one EASY
- (89) Angie didn't buy the car or the boat ... she bought both of them
- (88) Angie didn't buy the car or the boat ... she didn't want either one EASY
- (89) Angie didn't buy the car or the boat ... she bought both of them HARD

(90) Angie is not allowed to buy the car or the boat

(90) Angie is not allowed to buy the car or the boat ... she doesn't deserve either one

(90) Angie is not allowed to buy the car or the boat ... she doesn't deserve either one EASY

- (90) Angie is not allowed to buy the car or the boat ... she doesn't deserve either one EASY
- (91) Angie is not allowed to buy the car or the boat ...

- (90) Angie is not allowed to buy the car or the boat ... she doesn't deserve either one EASY
- (91) Angie is not allowed to buy the car or the boat ... she can only buy the car

- (90) Angie is not allowed to buy the car or the boat ... she doesn't deserve either one EASY
- (91) Angie is not allowed to buy the car or the boat ... she can only buy the car EASY

In sum

Promising direction to address the challenge for the implicature approach